

# Statistics

## Fall 2022

### Lecture 12



Feb 19-8:47 AM

A classroom has 18 females, and 12 males.

1)  $P(\text{Selecting a female}) = \frac{\text{Total female}}{\text{Total people}} = \frac{18}{30} = \boxed{\frac{3}{5}}$

2) odds in favor of selecting a female

$\# \text{ females} : \# \text{ Females} \rightarrow \boxed{3:2}$

3) odds  $\frac{18}{12}$  against selecting a female.

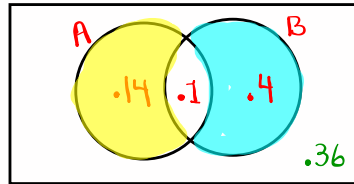
Reverse it

$\boxed{2:3}$

Nov 10-6:01 AM

Suppose  $P(A) = .24$ ,  $P(B) = .5$ ,  $P(A \text{ and } B) = .1$

1) Construct Venn Diagram.



overlap  
Total = 1  
 $1 - [.14 + .1 + .4] = .36$

2)  $P(A \text{ only}) = .24 - .1 = .14$

3)  $P(B \text{ only}) = .5 - .1 = .4$

4)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $= .24 + .5 - .1 = .64$

Use DeMorgan's Law to find

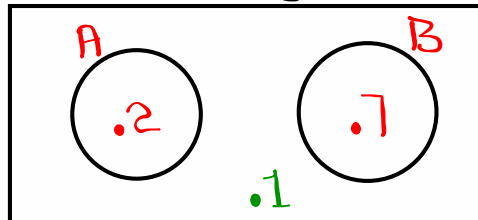
5)  $P(\bar{A} \text{ and } \bar{B}) = P(\overline{A \text{ or } B}) = 1 - P(A \text{ or } B) = 1 - .64 = .36$

6)  $P(\bar{A} \text{ or } \bar{B}) = P(\overline{A \text{ and } B}) = 1 - P(A \text{ and } B)$   
 $= 1 - .1 = .9$

Nov 10-6:06 AM

Suppose  $P(A) = .2$ ,  $P(B) = .7$ ,  $A \nabla B$  are

1) Construct Venn Diagram



M.E.E.

Mutually

Exclusive

Events

Total = 1  
 $1 - [.2 + .7] = .1$

2)  $P(\bar{A}) = 1 - P(A) = 1 - .2 = .8$

3)  $P(\bar{B}) = 1 - P(B) = 1 - .7 = .3$

3)  $P(A \text{ and } B) = 0$

4)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$   
 $= .2 + .7 - 0 = .9$

Nov 10-6:18 AM

Multiplication Rule (Sec 12 & 13)

keyword: AND

It is a multiple Action event

$$P(A \text{ and } B) = P(A) \cdot P(B|A)$$

A happens, then B happens ← Given

When events are independent events,

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

What are independent events?  
 outcome of one event does not change the prob. of next event.

$P(\text{Boy}) = .5$      $P(\text{Girl}) = .5$

First child is Boy  $\rightarrow P(\text{Boy}) = .5$

$P(\text{Next child is a boy}) = .5$

$P(\text{Next child is a girl}) = .5$

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Roll a fair die twice.

$P(\text{get 5 on first Roll}) = \frac{1}{6}$

$P(\text{get 5 on second Roll}) = \frac{1}{6}$

Nov 10-6:25 AM

A standard deck of playing cards has 52 cards, 26 Red, 12 face, 4 Aces.

Let's take 3 cards with replacement

$P(\text{First card is Ace}) = \frac{4}{52} = \frac{1}{13}$  Any card selected will be placed back in the deck

$P(\text{Second card is Ace}) = \frac{4}{52} = \frac{1}{13}$  before the next selection.

$P(\text{Third card is Face}) = \frac{12}{52} = \frac{3}{13}$

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A piggy bank has 4 quarters, 6 dimes, and 10 nickels. we take randomly 2 coins with replacement

|    |    |    |
|----|----|----|
| QQ | DQ | NQ |
| QD | DD | ND |
| QN | DN | NN |

Sample Space is a complete list of all possible outcomes

$P(\text{First coin is Quarter}) = \frac{4}{20} = \frac{1}{5}$

$P(\text{Second coin is Nickel}) = \frac{10}{20} = \frac{1}{2}$

Nov 10-6:34 AM

Class QZ 13

$$P(A) = .85$$

$$P(B) = .25$$

$$P(A \text{ and } B) = .2$$

$$1) P(\bar{A}) = 1 - P(A) = 1 - .85 = \boxed{.15}$$

$$\begin{aligned} 2) P(A \text{ or } B) &= P(A) + P(B) - P(A \text{ and } B) \\ &= .85 + .25 - .2 = \boxed{.9} \end{aligned}$$

Nov 10-6:48 AM

## Multiplication Rule

Part I: A and B are independent events

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

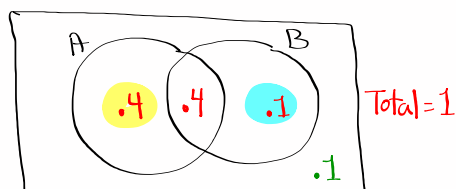
Ex:  $P(A) = .8$ ,  $P(B) = .5$ , A & B are independent events

$$1) P(\bar{A}) = 1 - P(A) = \boxed{.2}$$

$$2) P(\bar{B}) = 1 - P(B) = \boxed{.5}$$

$$3) P(A \text{ and } B) = P(A) \cdot P(B) = (.8)(.5) = \boxed{.4}$$

$$\begin{aligned} 4) P(A \text{ or } B) &= P(A) + P(B) - P(A \text{ and } B) \\ &= .8 + .5 - .4 = \boxed{.9} \end{aligned}$$



Nov 10-7:13 AM

$P(A) = .7$       1)  $P(\bar{A}) = 1 - P(A) = \boxed{.3}$   
 $P(B) = .4$       2)  $P(\bar{B}) = 1 - P(B) = \boxed{.6}$   
 A & B are Independent Events  
 3)  $P(A \text{ and } B) = P(A) \cdot P(B) = \boxed{.28}$   
 4)  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B) = .7 + .4 - .28 = \boxed{.82}$   
 5) make Venn Diagram

6)  $P(\text{A only OR B only}) = .42 + .12 = \boxed{.54}$   
 $P(A \text{ or } B \text{ not both})$

Nov 10-7:21 AM

A box has 3 Red and 7 Blue balls.  
 Randomly select 2 balls with replacement

Sample Space  
 RR    RB    BR    BB

$P(2 \text{ Red balls}) = \frac{3}{10} \cdot \frac{3}{10} = \frac{9}{100} = \boxed{.09}$   
 $P(1R \text{ \& } 1B) = P(RB \text{ or } BR) = 2 \left( \frac{3}{10} \cdot \frac{7}{10} \right) = \frac{42}{100} = \boxed{.42}$   
 $P(2 \text{ Blue balls}) = \frac{7}{10} \cdot \frac{7}{10} = \frac{49}{100} = \boxed{.49}$

Verify that Total Prob. = 1  
 $.09 + .42 + .49 = 1 \checkmark$

Nov 10-7:32 AM

Standard deck of playing cards has  
52 cards, and 4 Aces.

Draw 2 cards **with replacement.**

Sample Space  $A \rightarrow \text{Ace}$   
 $AA \quad A\bar{A} \quad \bar{A}A \quad \bar{A}\bar{A}$

$$P(2 \text{ Aces}) = P(AA) = \frac{4}{52} \cdot \frac{4}{52} = \frac{1}{13} \cdot \frac{1}{13} = \frac{1}{169}$$

$$P(1A \& 1\bar{A}) = P(A\bar{A} \text{ or } \bar{A}A) = 2 \left( \frac{4}{52} \cdot \frac{48}{52} \right) = \frac{24}{169}$$

$$P(\text{No Aces}) = P(\bar{A}\bar{A}) = \frac{48}{52} \cdot \frac{48}{52} = \frac{12}{13} \cdot \frac{12}{13} = \frac{144}{169}$$

Verify that Total Prob. = 1

$$1 \div 169 + 24 \div 169 + 144 \div 169 \text{ [enter]} = 1$$

Nov 10-7:43 AM

There are 2 Dimes and 3 Nickels in a piggy bank.

randomly take 2 coins **with replacement**

$D \rightarrow \text{Dimes}$ ,  $N \rightarrow \text{Nickels}$

1) Sample Space

$DD \quad DN \quad ND \quad NN$

$$2) P(\text{Total is } 10\text{¢}) = P(NN) = \frac{3}{5} \cdot \frac{3}{5} = \frac{9}{25} = 0.36 \checkmark$$

$$3) P(\text{Total is } 15\text{¢}) = P(DN \text{ or } ND) = 2 \left( \frac{2}{5} \cdot \frac{3}{5} \right) = 0.48 \checkmark$$

$$4) P(\text{Total is } 20\text{¢}) = P(DD) = \frac{2}{5} \cdot \frac{2}{5} = \frac{4}{25} = 0.16 \checkmark$$

Verify that Total Prob. = 1

| Total | P(Total) |
|-------|----------|
| 10¢   | .36      |
| 15¢   | .48      |
| 20¢   | .16      |

clear all lists

Total  $\rightarrow$  L1

P(Total)  $\rightarrow$  L2

use **1-Var Stats** with **L1:L2**  
to find

$$\bar{x} = 14$$

$S_x =$  blank

$$n = 1 \leftarrow \text{Total prob.} = 1$$

Nov 10-7:55 AM

There are 4 Red, 6 Blue, and 10 white balls in a box.

$$1) P(\text{select a blue ball}) = \frac{6}{20} = \frac{3}{10} = .3$$

2) Odds in favor of Selecting blue ball.

$$\# \text{ Blue} : \# \text{ Blue} \rightarrow 3 : 7$$

$$6 : 14$$

3) odds against Selecting a red ball.

$$\# \text{ Red} : \# \text{ Red} \rightarrow 4 : 1$$

$$16 : 4$$

4) odds in favor of Selecting a white ball.

$$\# \text{ white} : \# \text{ white} \rightarrow 1 : 1$$

$$10 : 10$$

Nov 10-8:11 AM

Suppose  $P(A) = .04$

$$1) P(\bar{A}) = 1 - P(A) = .96$$

2) odds in favor of event A.

$$P(A) : P(\bar{A}) \rightarrow 1 : 24$$

$$.04 : .96$$

3) odds against event A.

Reverse it

$$24 : 1$$

Nov 10-8:22 AM

Suppose odds in favor of event A are

$$\begin{array}{cc} 3 & 47 \\ a & b \end{array}$$

1) odds against A  $\boxed{47:3}$

$$\begin{aligned} 2) P(A) &= \frac{a}{a+b} = \frac{3}{3+47} = \boxed{\frac{3}{50}} \\ &= \boxed{.06} \end{aligned}$$

$$\begin{aligned} 3) P(\bar{A}) &= \frac{b}{a+b} = \frac{47}{3+47} \\ &= \boxed{\frac{47}{50}} \\ &= \boxed{.94} \end{aligned}$$

Nov 10-8:25 AM